

# Computational Thinking

**Jeannette M. Wing**

Avanessians Director of the Data Science Institute and Professor of Computer Science,  
Columbia University

Consulting Professor of Computer Science, Carnegie Mellon University

# My Grand Vision

- **Computational thinking** will be a fundamental skill used by everyone in the world by the middle of the 21<sup>st</sup> Century.
  - Just like reading, writing, and arithmetic.
  - Incestuous: Computing and computers will enable the spread of computational thinking.
  - **In research:** scientists, engineers, ..., historians, artists
  - **In education:** K-12 students and teachers, undergrads, ...

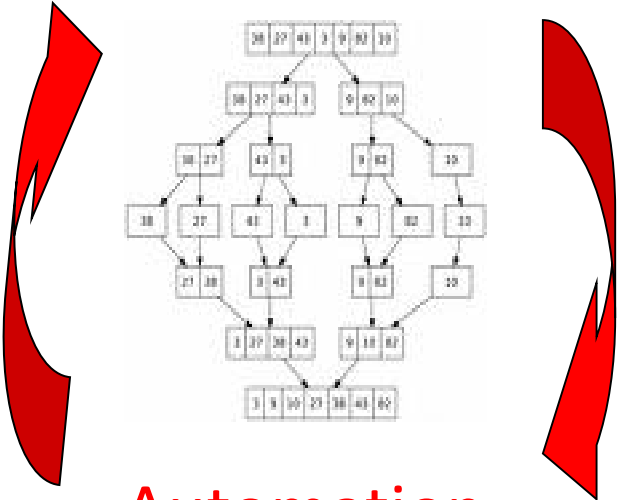
J.M. Wing, "Computational Thinking," *CACM Viewpoint*, March 2006, pp. 33-35.  
Paper off <http://www.cs.cmu.edu/~wing/>

# What is Computational Thinking?

Computational thinking is the *thought processes* involved in formulating a problem and expressing its solution(s) in such a way that a computer—human or machine—can effectively carry out.

# The Critical Thought Process: Abstraction

Abstractions



Automation

# Computational Thinking, Philosophically

- Complements and combines mathematical and engineering thinking
  - C.T. draws on math as its foundations
    - But we are constrained by the physics of the underlying machine
  - C.T. draws on engineering since our systems interact with the real world
    - But we can build virtual worlds unconstrained by physical reality
- Ideas, not artifacts
  - It's not just the software and hardware that touch our daily lives, it will be the computational concepts we use to approach living.
- It's for everyone, everywhere

# Sample Classes of Computational Concepts

- Algorithms
  - E.g., mergesort, binary search, string matching, clustering
- Data Structures
  - E.g., sequences, tables, trees, graphs, networks
- State Machines
  - E.g., finite automata, Turing machines
- Languages
  - E.g., regular expressions, ..., VDM, Z, ..., ML, Haskell, ..., Java, Python
- Logics and semantics
  - E.g., Hoare triples, temporal logic, modal logics, lambda calculus
- Heuristics
  - E.g., A\* (best-first graph search), caching
- Control Structures
  - Parallel/sequential composition, iteration, recursion
- Communication
  - E.g., synchronous/asynchronous, broadcast/P2P, RPC, shared memory/message-passing
- Architectures
  - E.g., layered, hierarchical, pipeline, blackboard, feedback loop, client-

## NOT

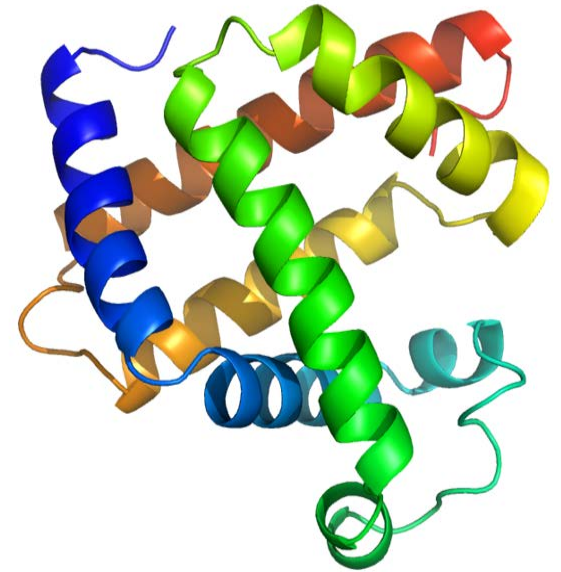
- Computer literacy, i.e., how to use Word or Excel
- Computer programming, i.e., beyond Java Programming 101

# Examples of Computational Thinking in Other Disciplines

**One Discipline, Many Computational  
Methods**



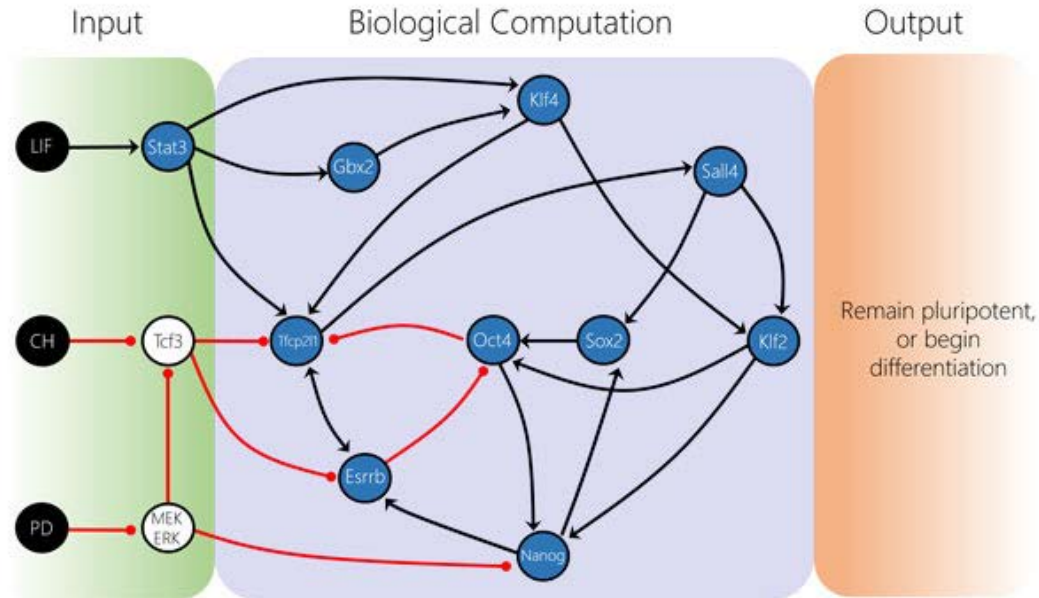
# Computational Thinking in Biology



- Shotgun **algorithm** expedites sequencing of human genome
- **Abstract interpretation** in systems biology
- **Model checking** applied to arrhythmia, diabetes, pancreatic cancer
- DNA sequences are strings in a **language**
- **Boolean networks** approximate dynamics of biological networks
- Cells as a self-regulatory system are like **electronic circuits**
- **Process calculi** model interactions among molecules
- **Statecharts** used in developmental genetics
- Protein kinetics can be modeled as **computational processes**
- **Robot Adam** discovers role of 12 genes in yeast
- PageRank **algorithm** inspires ecological food web

Insight: Models and languages for expressing computational processes are good for expressing the dynamics of biological processes.

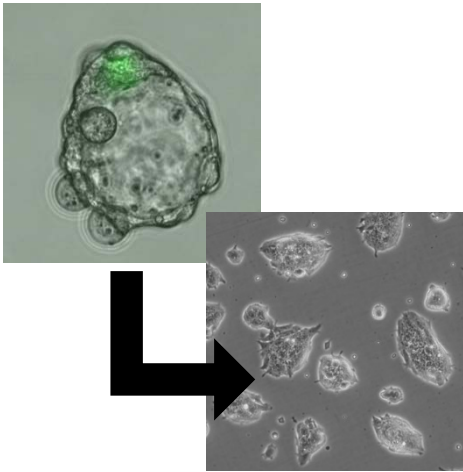
# Stem Cell Prediction



[Dunn et al., "Defining an essential transcription factor program for naïve pluripotency," *Science*, June 2014, pp. 1156-1160]

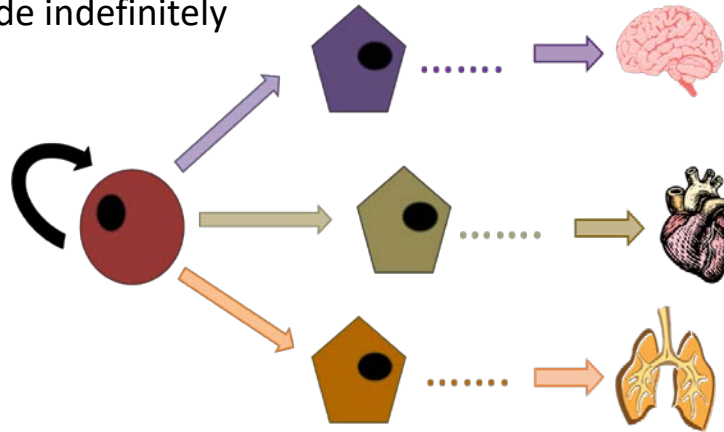


# Embryonic Stem (ES) Cells

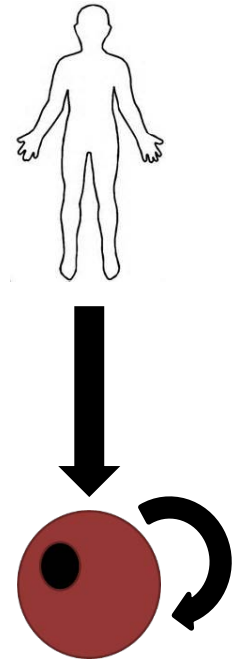


**Transient in tissue:**  
A culture-dependent phenomenon

**Self-renewing:**  
Divide indefinitely



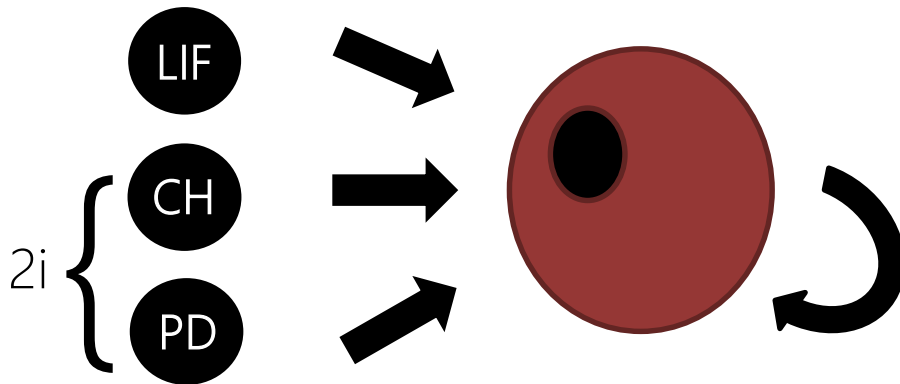
**Pluripotent:** Generate all adult cell types, and can be re-injected back into the developing embryo



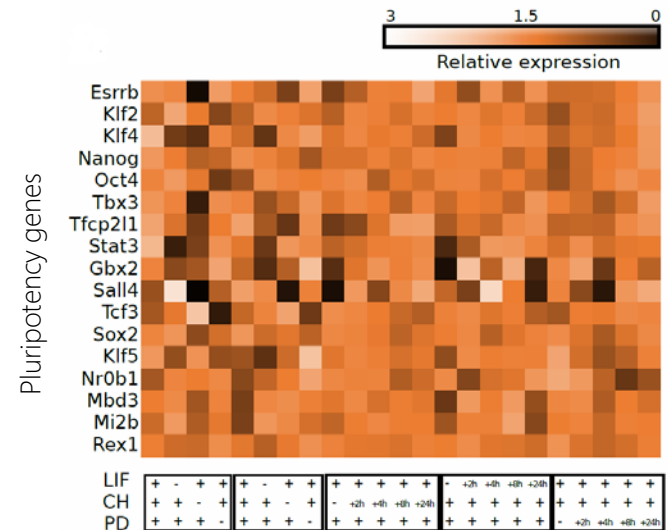
We can **reprogram** adult cells to this state

# Extrinsic Signals Control ES Cell Behavior

Whether an ES cell will remain self-renewing, or differentiate towards an adult cell lineage depends on the signals that it receives.

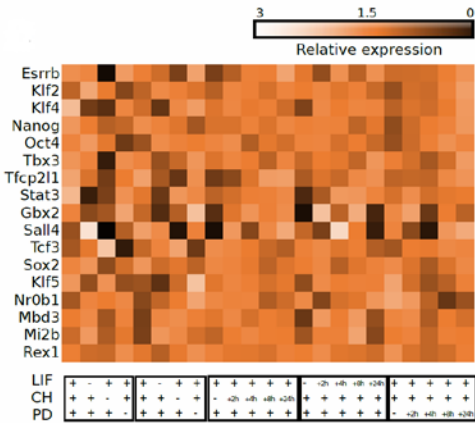


The signals required to sustain ES cells in culture have been progressively refined. Any two of LIF, CH and PD are sufficient.

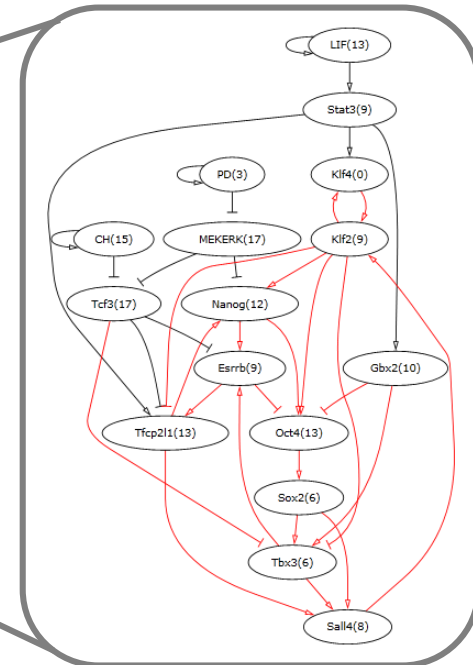
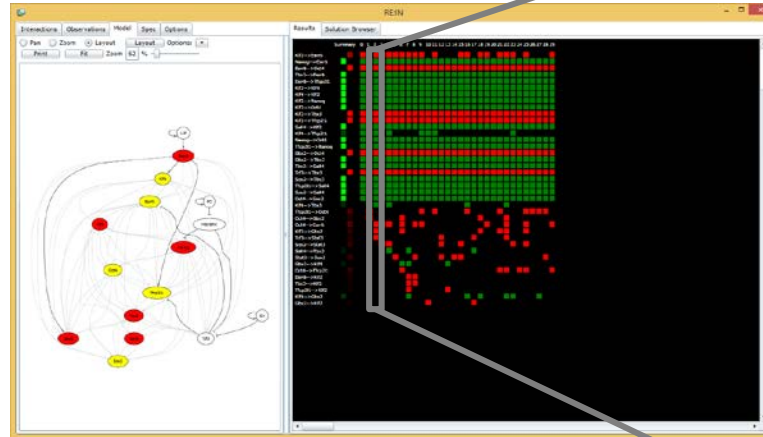
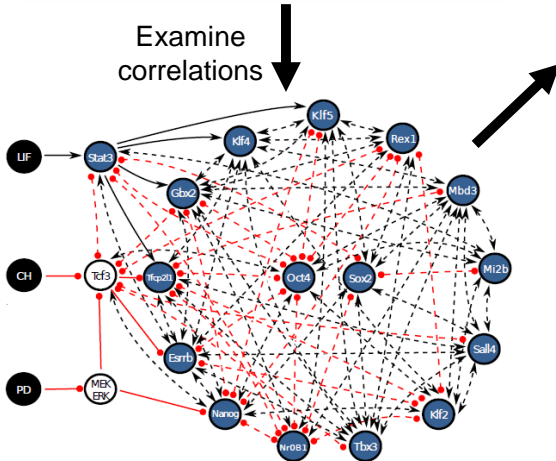


We can measure the expression of key genes under different combinations of signals to gain insight into the dynamic behavior of the system.

# A Reasoning Engine for Interaction Networks



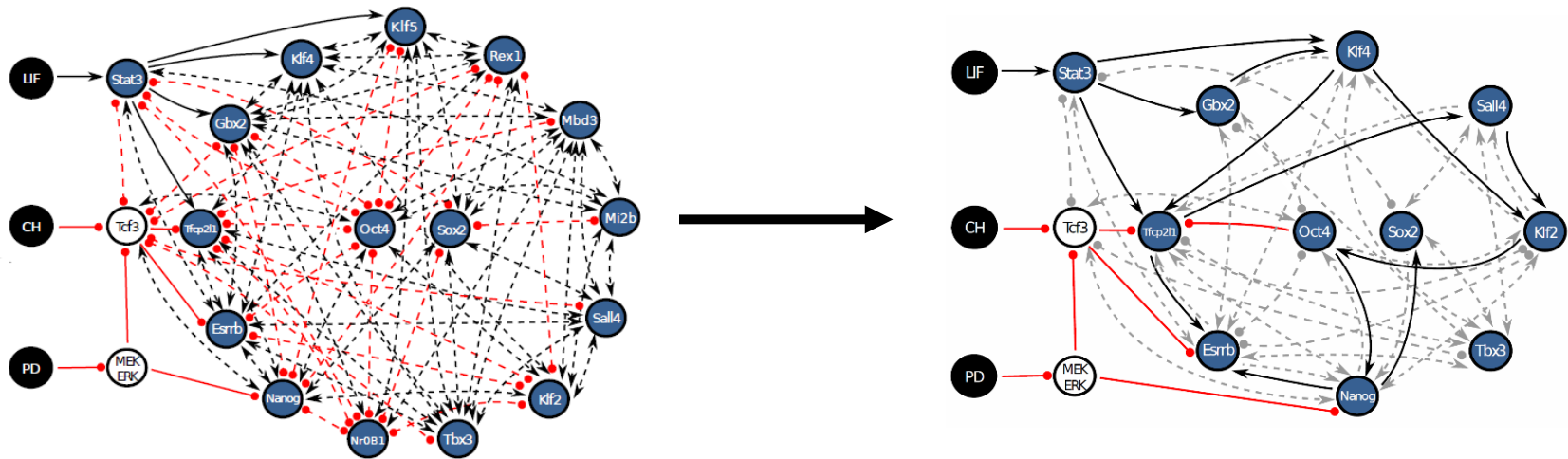
Examine correlations



RE:IN is a tool built on Z3 that utilizes Satisfiability Modulo Theories to synthesize only those (out of  $10^{43}$ ) Boolean networks that provably satisfy experimental constraints.

IF (signalA AND signalB AND NOT signalC OR ...)  
THEN remain a stem cell  
ELSE (IF NOT signalA ...)  
differentiate

# Biological Computation in Stem Cells



- The set of possible models was constrained by experimentally-observed behaviours
- This set was used to make a large number (53) of non-intuitive predictions of the response of the network to genetic perturbations. These predictions were experimentally validated with over 70% accuracy rate.
- The highlighted interactions show the minimal set required to explain stem cell behaviour: **the essential program governing naïve pluripotency**

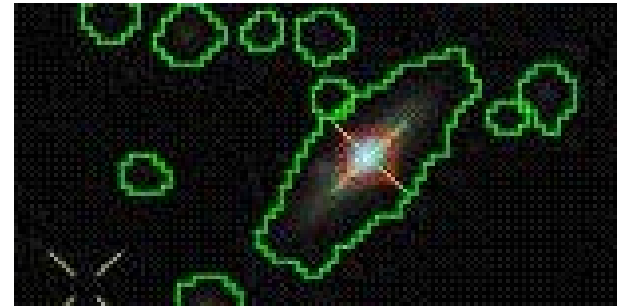
# One Computational Method, Many Disciplines

Machine Learning has transformed the field of Statistics.

# Machine Learning in the Sciences

## Astronomy

- Brown dwarfs and fossil galaxies discovery via machine learning, data mining, data federation
- Very large multi-dimensional datasets analysis using KD-trees



Credit: SDSS

## Medicine



- Anti-inflammatory drugs
- Chronic hepatitis
- Mammograms
- Renal and respiratory failure

Credit: LiveScience

## Meteorology

- Tornado formation



© Copyright 2004 Eric Nguyen

## Neurosciences

- fMRI data analysis to understand language via machine learning





# Machine Learning Everywhere



Credit Cards



Supermarkets



Wall Street

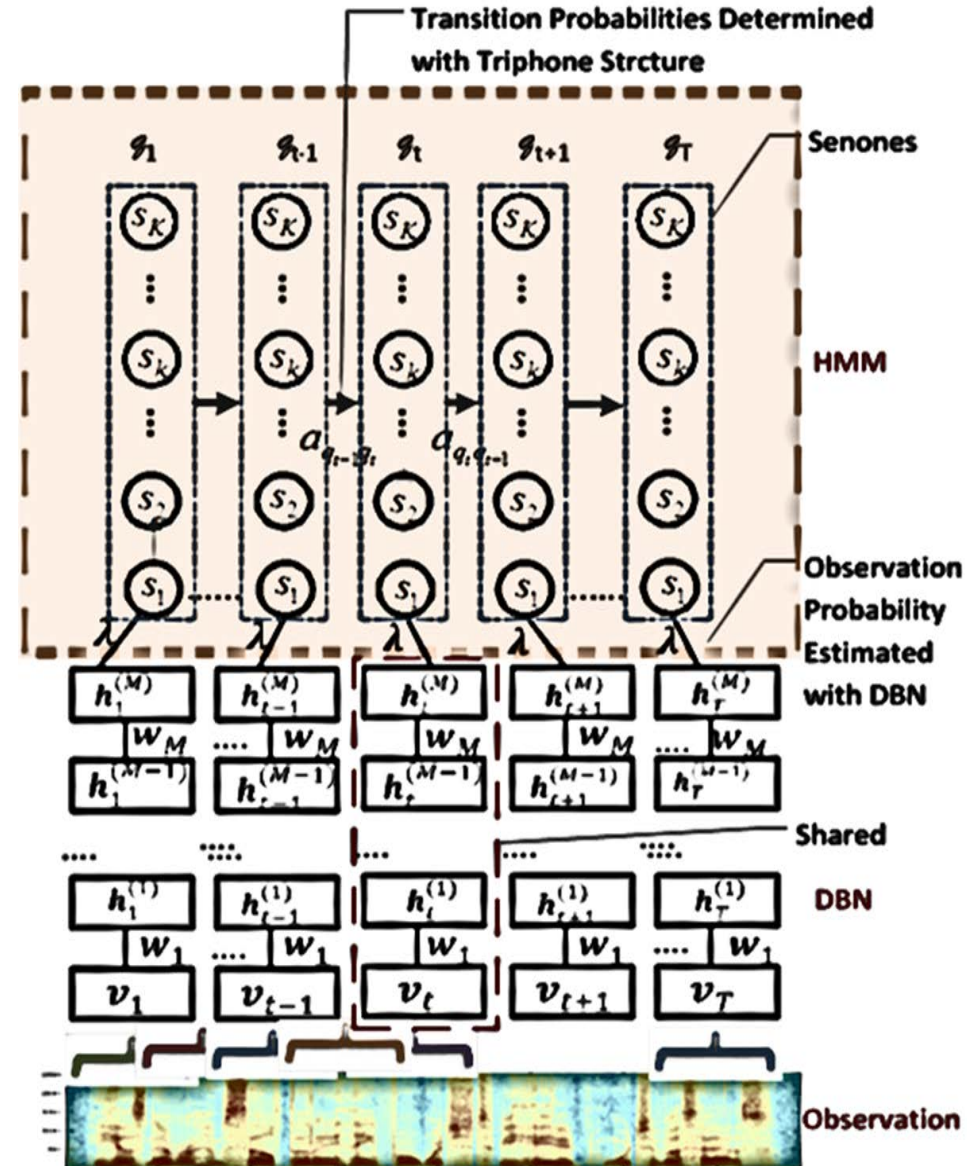
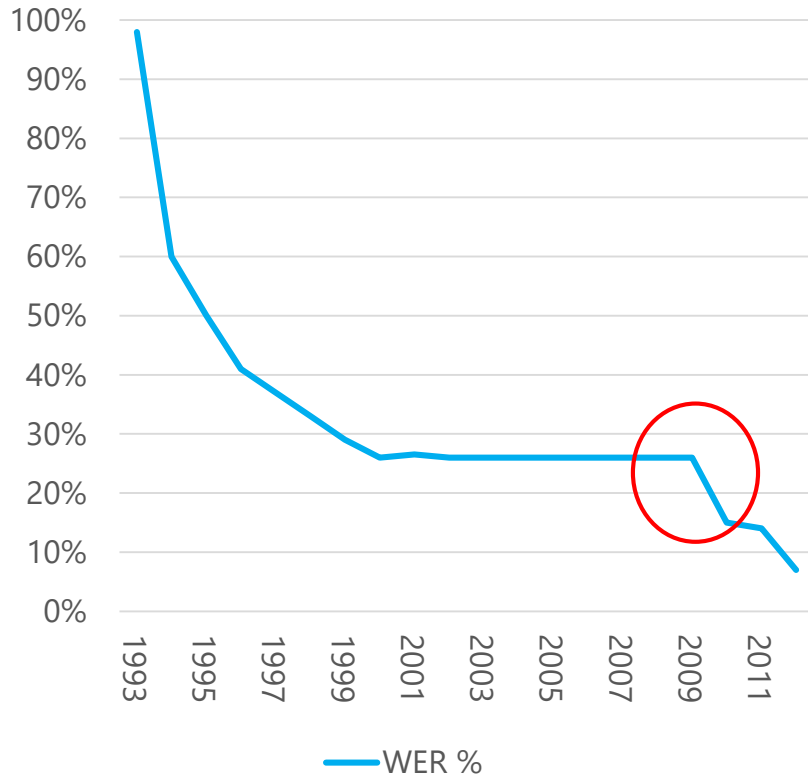
Entertainment:  
Shopping, Music, Travel



Sports



# Deep Neural Networks



# Speech-to-Speech



Tianjin, China, October 2012

English speech **of speaker**

→ English text

→ Chinese text

→ Chinese speech of **same speaker**

# Skype Translator: Breaking the Language Barriers

December 2014



Stafford Elementary  
Tacoma, Washington, USA

Colegio Peterson  
Mexico City, Mexico



# Historic Achievement: Microsoft researchers reach human parity in conversational speech recognition



## **Achieving Human Parity in Conversational Speech Recognition**

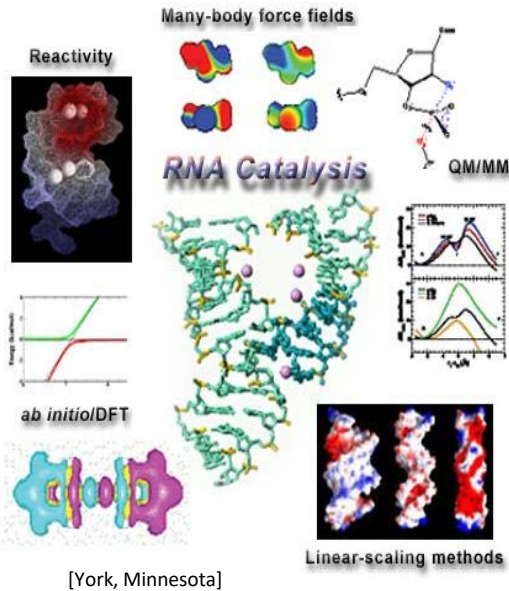
W. Xiong, J. Droppo, X. Huang, F. Seide, M. Seltzer, A. Stolcke, D. Yu, G. Zweig

*(Submitted on 17 Oct 2016)*

# Computational Thinking in the Sciences and Beyond

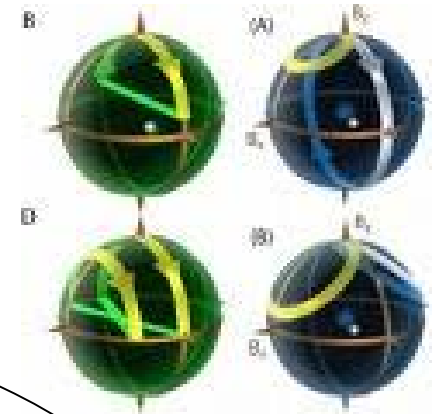
# Computational Thinking in Other Sciences

## Chemistry



- Atomistic calculations are used to explore chemical phenomena
- Optimization and searching algorithms identify best chemicals for improving reaction conditions to improve yields

## Physics



- Adiabatic quantum computing: How quickly is convergence?
- Genetic algorithms discover laws of physics.

## Geosciences

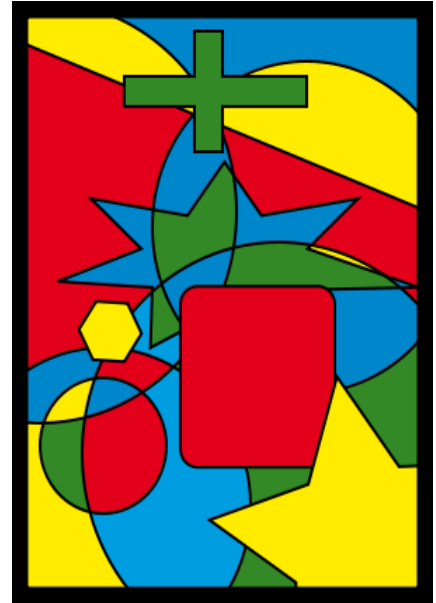
- DeepDive: analysis of measurement info buried in geoscience literature
- Cornell's NSF Expedition on Computational Sustainability
- FetchClimate from MSR: predictive analysis of multiple large datasets



# Computational Thinking in Math and Engineering

## Mathematics

- Discovering E8 Lie Group:  
18 mathematicians, 4 years and 77 hours of  
supercomputer time (200 billion numbers).  
Profound implications for physics (string theory)
- Four-color theorem proof



Credit: Wikipedia

Credit: Wikipedia

## Engineering (electrical, civil, mechanical, aero & astro,...)

Credit: Boeing



- Calculating higher order terms implies more precision,  
which implies reducing weight, waste, costs in fabricati
- Boeing 777 tested via computer simulation alone,  
not in a wind tunnel
- Hybrid automata for modeling and analyzing  
cyber-physical systems



# Computational Thinking for Society

Microsoft Digital Advertising Solutions

## Economics



- Automated mechanism design underlies electronic commerce, e.g., ad placement, on-line auctions, kidney exchange
- Internet marketplace requires revisiting Nash equilibria model
- Use intractability for voting schemes to circumvent impossibility results

- Inventions discovered through automated search are patentable
- Stanford CL approaches include AI, temporal logic, state machines, process algebras, Petri nets
- POIROT Project on fraud investigation is creating a detailed ontology of European law
- Sherlock Project on crime scene investigation

## Law



## Healthcare

- Algorithmic medicine
- Software design principles and debugging applied to prescriptions of painkillers
- ONC SHARP Program, NSF Smart Health and Wellness Program, NITRD Senior Steering Group on Health IT



# Computational Thinking for Society

## Archaeology

- eHeritage Project, Microsoft Research Asia
- Digital Forma Urbis Romae Project, Stanford
- Cathedral Saint Pierre, Columbia



- Crowd sourcing as a new way of getting news tips from sources
- Algorithmic approach to validate credibility of sources
- Digital Media and Learning Initiative, MacArthur Foundation

## Journalism



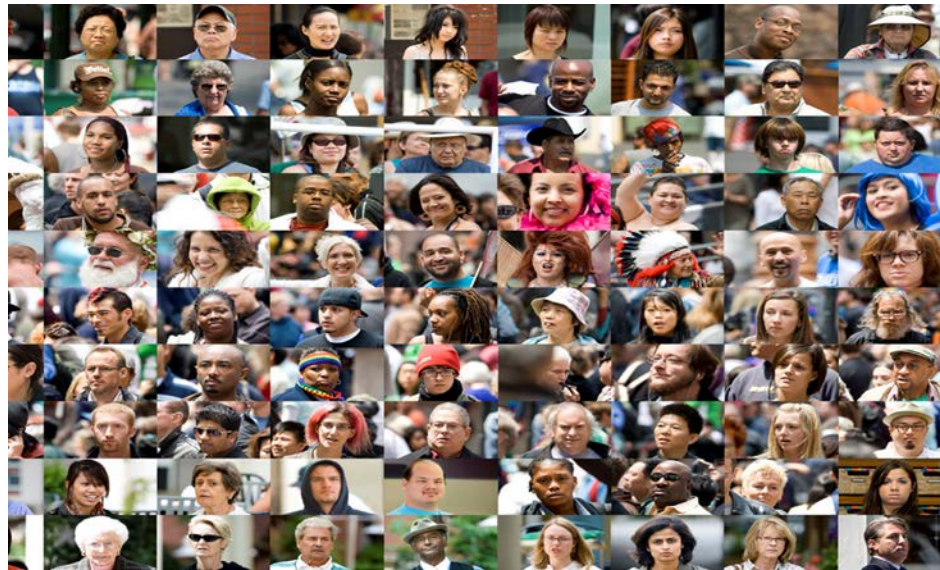
## Humanities

- Digging into Data Challenge: What could you do with a million books?  
Nat'l Endowment for the Humanities (US),  
JISC (UK), SSHRC (Canada)
- Music, English, Art, Design, Photography, ...



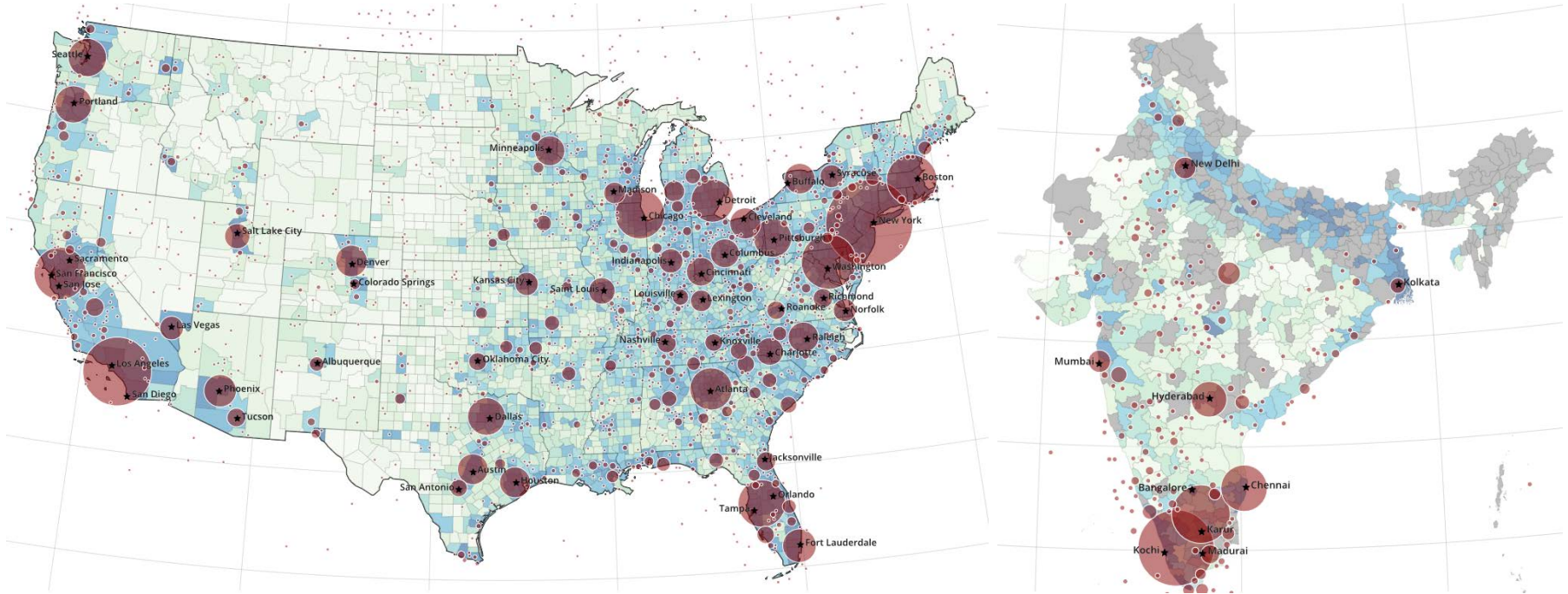
# Computational Social Science: Learning about Crowdworkers

- Computational: digital studies produce the *nodes* (people) and *edges* (relationships) in a network



- Anthropology: qualitative studies produce the *variety of nodes* (individuals, institutions) and *meaning of edges* (motivations, hierarchies, power dynamics)

# Mapping the Crowd

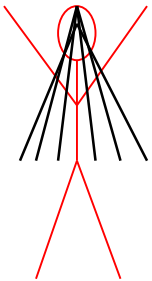
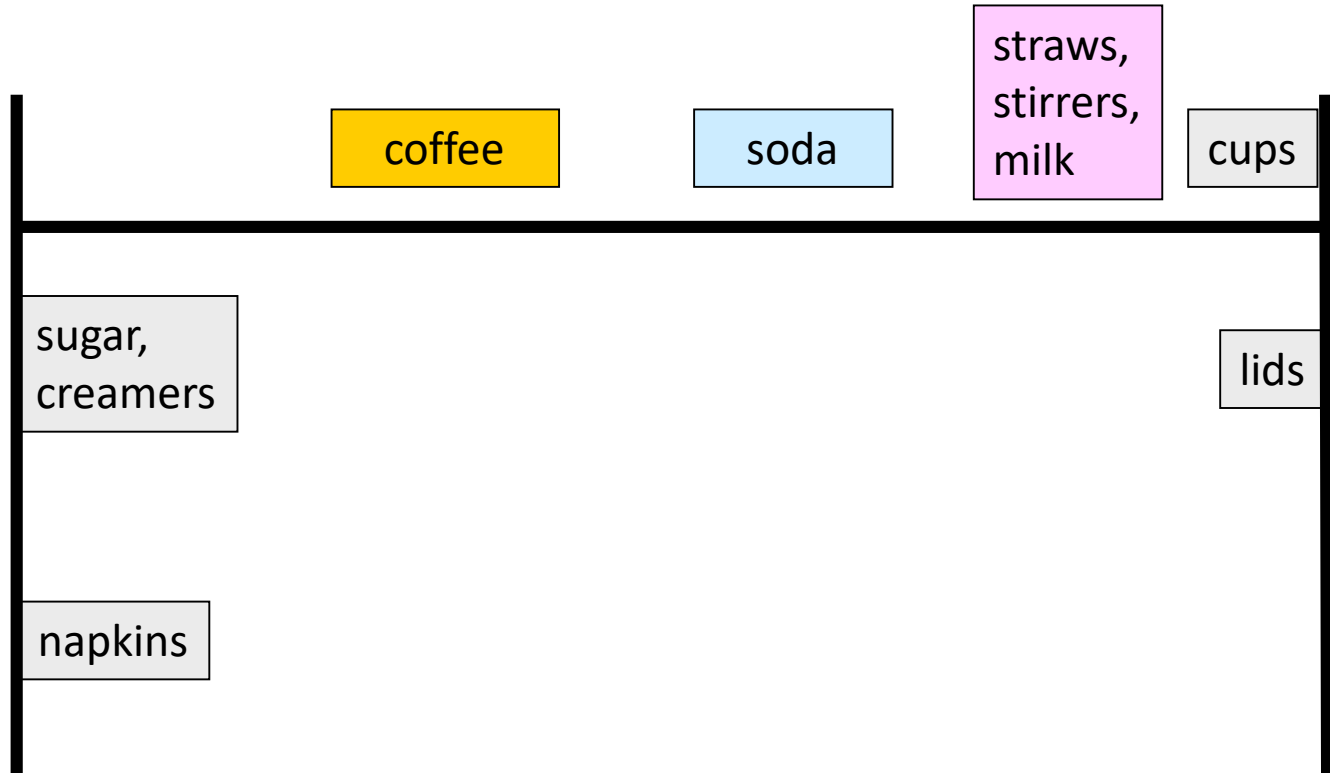


Self-reported locations for ~10,000 participants in a map task on Amazon Mechanical Turk. Coloration of counties/districts is by *population density*.

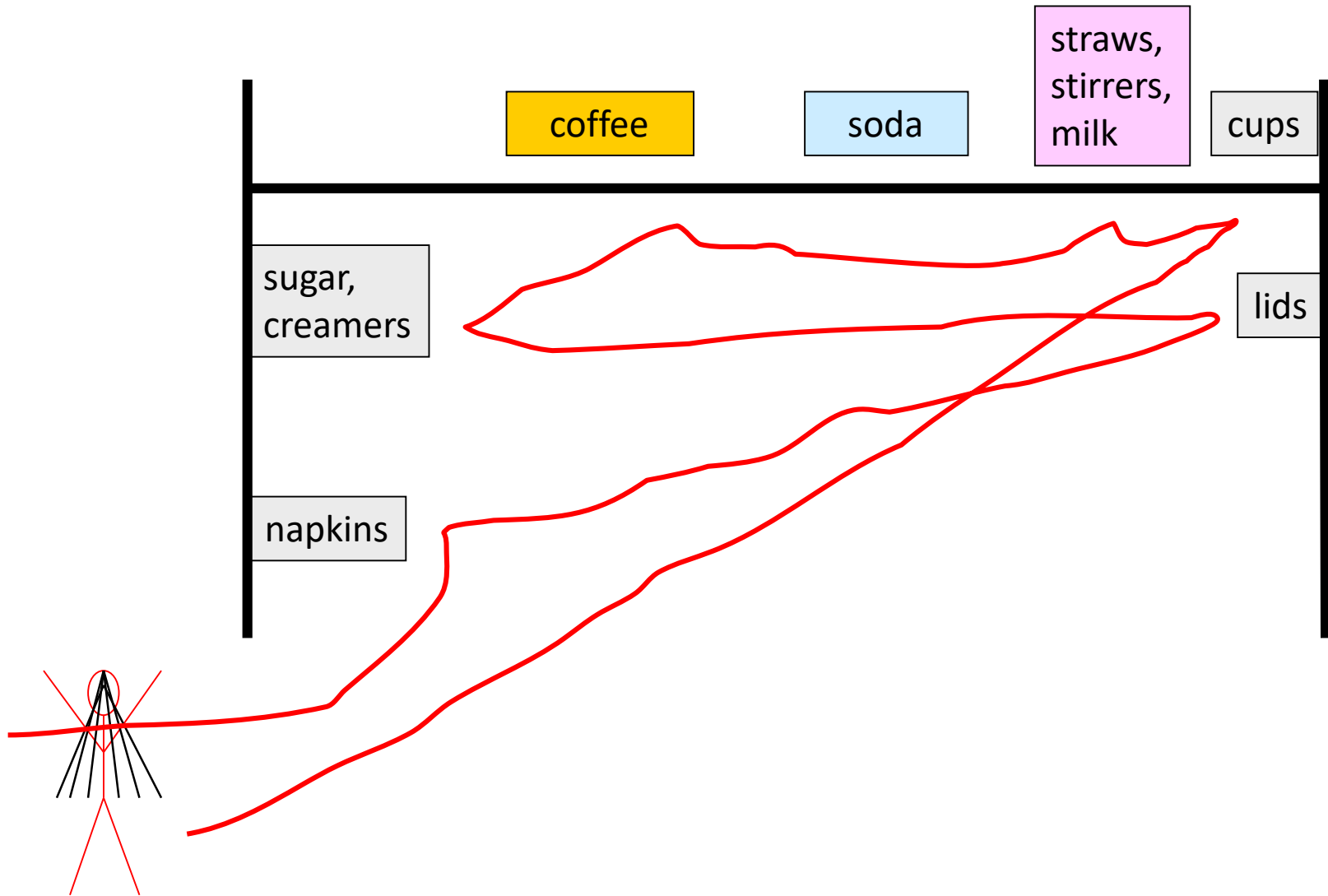
Data supports Theory of Imperfect Competition

# Computational Thinking in Daily Life

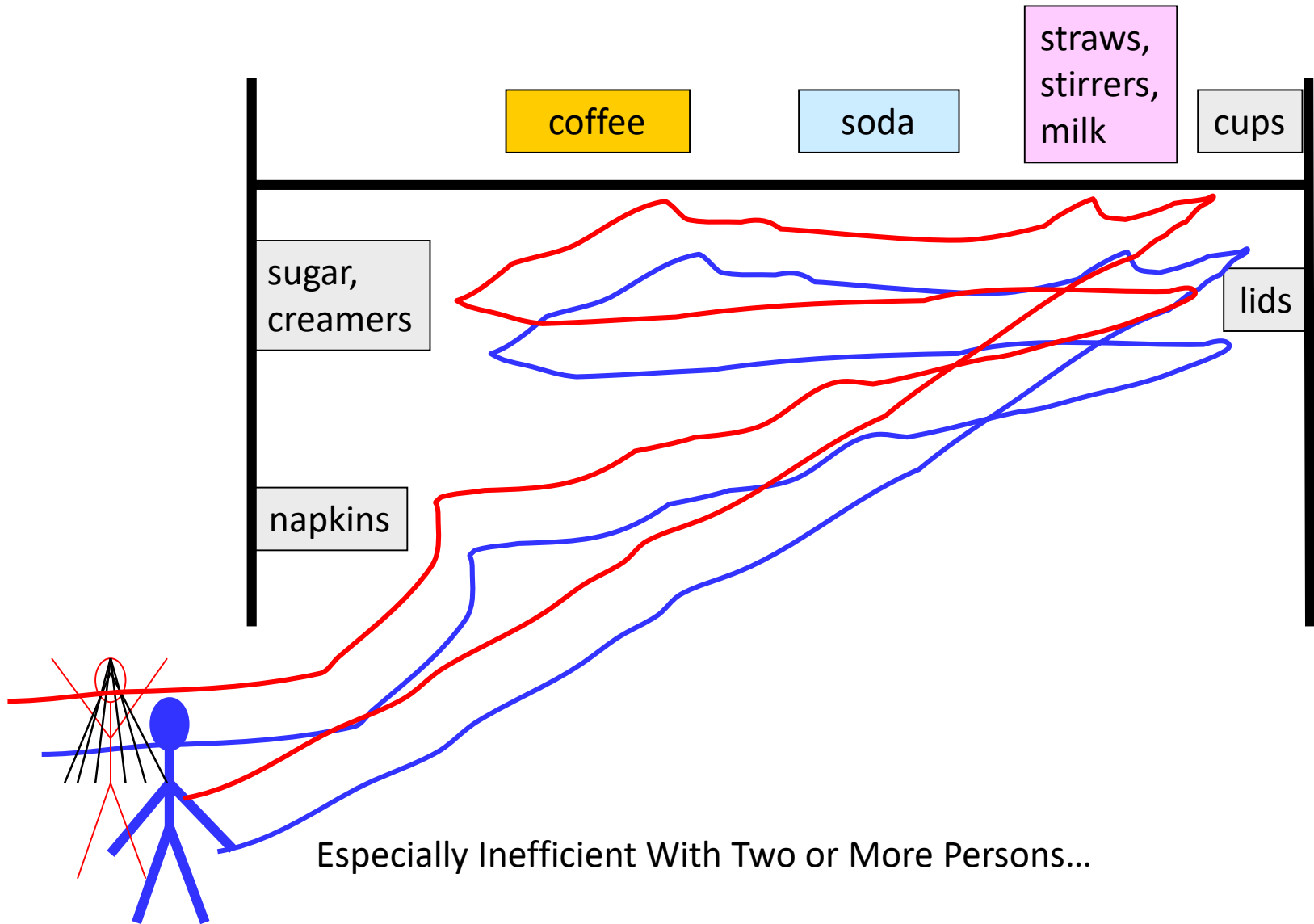
# Getting Morning Coffee at the Cafeteria



# Getting Morning Coffee at the Cafeteria

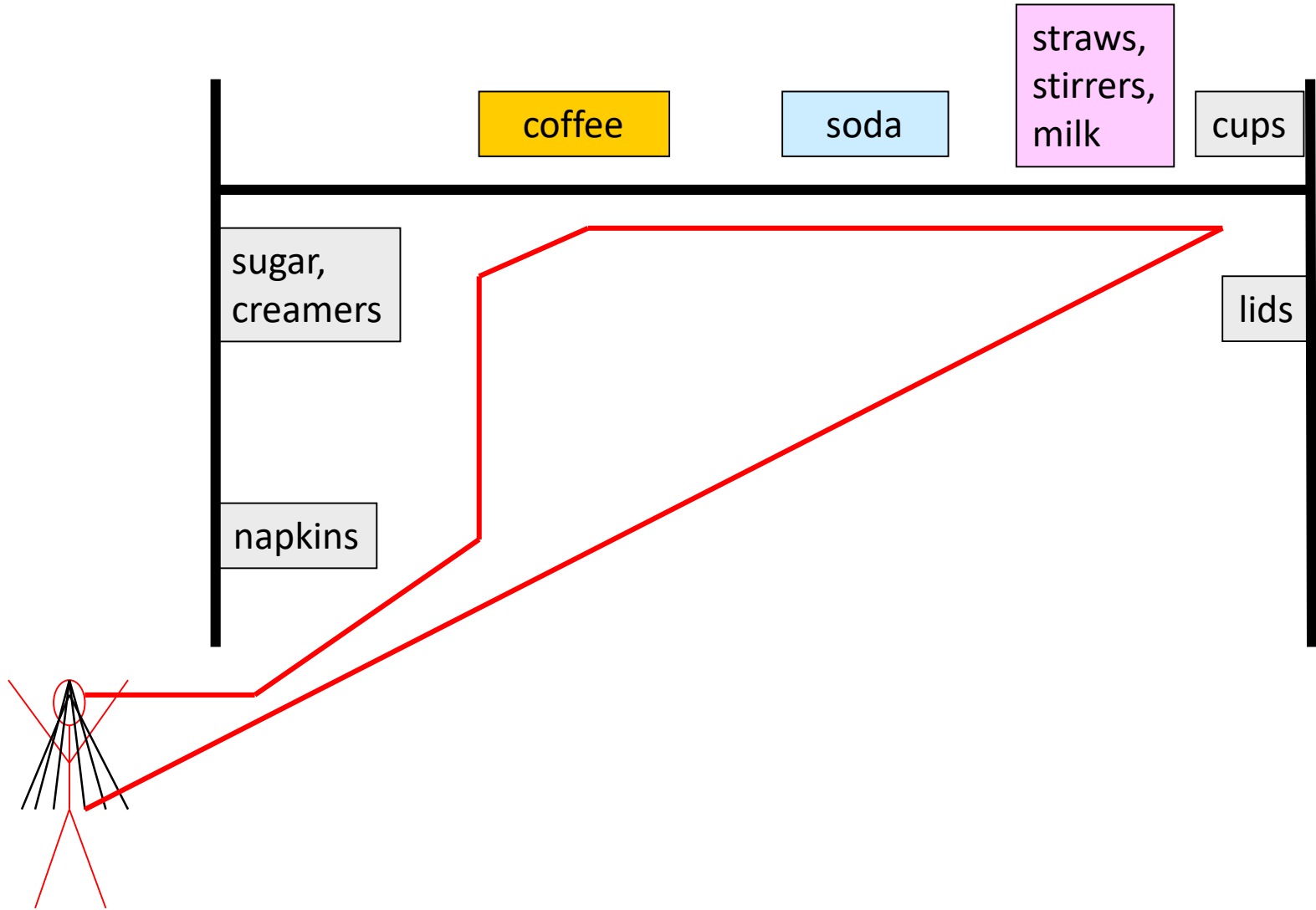


# Getting Morning Coffee at the Cafeteria





# Better: Think Computationally—Pipelining!



# Computational Thinking in Education

# Education Implications for K-12

## Question and Challenge for the Computing Community:

What is an effective way of learning (teaching) computational thinking by (to) K-12?

- What concepts can students (educators) best learn (teach) when?  
What is our analogy to numbers in K, algebra in 7, and calculus in 12?
- We uniquely also should ask how best to integrate The Computer with teaching the concepts.

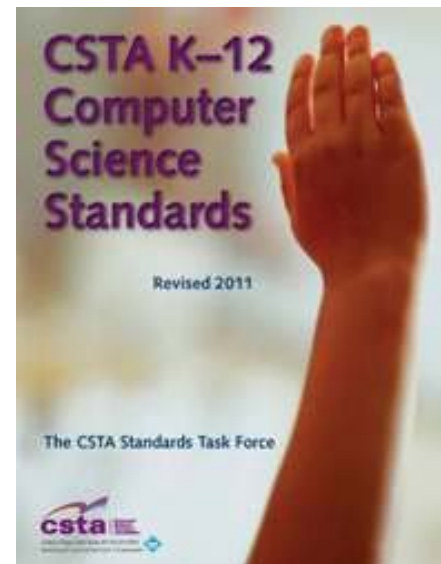
Computer scientists are now working with educators and cognitive learning scientists to address these questions.

# United States Efforts

## High School



CS Principles: <http://csprinciples.org>  
- With NSF support, revision of CS AP courses



## K-12

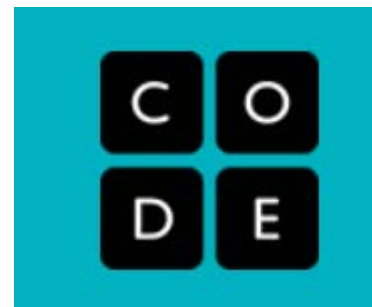


<http://www.csta.acm.org/>

- *Computational Thinking Resource Set: A Problem-Solving Tool for Every Classroom*
- K-12 Computer Science Standards

[www.code.org](http://www.code.org)

- non-profit to ensure CS is available to all high school students



## Congress

Computer Science Education Act ([H.R.5929](https://www.congress.gov/bills/111/5929)) 2010  
- proposed by PA Senator Casey and CO Representative Polis.



# US Goal: Give Access to Computer Science to Every High School Student

City of Chicago The City of Chicago's Official Site

Home City Services People We Serve Programs & Initiatives Chicago Government About Chicago

Chicago: HS graduation requirement by 2018.

The New York Times

De Blasio to Announce 10-Year Deadline to Offer Computer Science to All Students

New York City: CS for all within 10 years.

CS4RI  
Computer Science for Rhode Island

Rhode Island: CS taught in every public school by December 2017.

WASHINGTON STATE  
REIMAGINING SCIENCE ENGINEERING + MATHEMATICS

Washington State: K-12 CS standards, teacher support

GOVERNOR INSLEE SIGNS LAW TO EXPAND COMPUTER SCIENCE EDUCATION

For Immediate Release  
June 10, 2015  
SEATTLE, Wash. – Today, Governor Jay Inslee signed Substitute House Bill 1813, which requires all public schools to offer computer science classes across the state and providing new access to what has become a focal point of Washington's economy.

SFUSD SAN FRANCISCO PUBLIC SCHOOLS

Board Approves Plans to Expand Computer Science Curriculum to All Grades

San Francisco: pre-K to HS, mandatory through 8<sup>th</sup> grade.

SET BIG GOALS  
GET ALIGNED  
BUILD A LEGACY  
ENGAGE THE TEAM  
BEAT THE QUARTER

# President Obama 2016 State of the Union Address



NSF funds \$25M for Computer Science for All with a commitment of \$100M more over the next four years.

"In the coming years, we should build on that progress, by providing pre-K for all, offering every student the hands-on computer science and math classes that make them job-ready on day one." [Obama, January 12, 2016]

# United Kingdom Efforts

## British Royal Society (2012): *Shut down or restart? report*



“Computational thinking” offers insightful ways to view how information operates in many natural and engineered systems.

...

3. Every child should have the opportunity to learn Computing at school. We believe that:

- Every child should be expected to be ‘digitally literate’ by the end of compulsory education, in the same way that every child is expected to be able to read and write. “

# Computing At School (K-12)

**COMPUTING AT SCHOOL**  
EDUCATE · ENGAGE · ENCOURAGE  
In collaboration with BCS, The Chartered Institute for IT

Establish computer science as a foundational subject discipline, like math or physics, that every child should learn, from primary school onwards.



An entirely new K-12 subject,  
Computer Science,  
started in England, Sept 2014.



# Other International Efforts



China



Australia



Germany



Korea



India



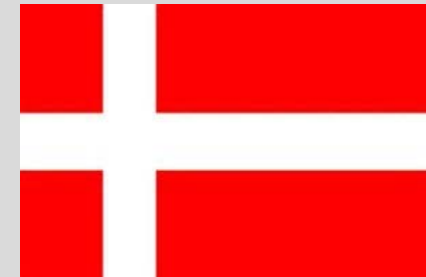
Finland



Singapore



Israel



Denmark



Belgium

Sweden?



# Computational Thinking, International

## 计算思维

周以真



计算思维代表着一种普遍的认识和一类普适的技能，每一个人，而不仅仅是计算机科学家，都应热心于它的学习和运用。

计

算思维建立在计算过程的能力和限制之上，由人由机器执行。计算方法和模型使我们敢于去处理那些原本无

一步问：一个近似解是否就足够了，是否可以利用一下随机化，以及是否允许误报 (false positive) 和漏报 (false negative)？计算思维

Jeannette M. Wing

## Computational Thinking – Informatisches Denken<sup>1</sup>

Übersetzung: Hermann Hellwagner (AAU Klagenfurt), Gerti Kappel und Radu Grosu (TU Wien)

*Informatisches Denken stellt eine universell einsetzbare Haltung und Fähigkeit dar, die alle lernen und nutzen sollten, nicht nur Informatiker.*

COMMUNICATIONS OF THE ACM March 2006/Vol. 49, No. 3

## 컴퓨팅적 사고

컴퓨팅적 사고는 컴퓨터 과학자뿐만 아니라 누구나 배워서 활용할 수 있는 보편적인 사고이자 기술이다.

컴퓨팅적 사고는 사고의 주체가 컴퓨터인 사물인간 간에 전산처리의 힘과 한계에 기반해 있다. 컴퓨팅적 방법론과 모델을 통해 우리는 혼자서는 만들 수 없는 시스템을 설계하고 어려운 문제를 해결할 수 있을 거라는 자신감을 얻을 수 있다. 우리는 컴퓨팅적 사고를 통해 수수께끼와 같은 기계 지능의 난제에 도전한다. 이를 이용하는 것이 용이한지, 거짓 양성 (false positives)과 거짓 음성 (false negatives)<sup>[2]</sup>을 허락해도 될지 고민할 것이다. 우리는 컴퓨팅적 사고를 통해 축소, 내강, 변형이나 시뮬레이션과 같은 기법으로 무척이나 어려워 보이는 문제를 이미 해결 방법을 알고 있는 문제로 재구성할 수도 있다.

In *Bulletin of Specif*, December 2008

## La pensée informatique

par Jeannette M. Wing

Cet article fait suite aux divers interviews que nous avons faits et qui nous invitaient à une réflexion sur les fondements de notre discipline et ses aspects philosophiques et épistémologiques. Aujourd'hui l'article de Jeannette Wing nous conduit à réfléchir sur l'utilité et l'ubiquité de la pensée informatique et ses implications, mais aussi sur l'essence même de cette pensée.

Computational Thinking – Jeannette Wing

*Communications of the ACM* vol. 49, n° 3, Mars 2006, pp. 33-35

## Il Pensiero Computazionale

Il pensiero computazionale si basa sul potere e sui limiti dei processi di elaborazione, siano essi eseguiti da un essere umano o da un macchina. I metodi ed i modelli computazionali ci danno il

[www.cs.cmu.edu/0002-2002-1013-1990](http://www.cs.cmu.edu/0002-2002-1013-1990)  
Carnegie Mellon University, Pennsylvania,  
1 Institute Creator

**PENSAMENTO COMPUTACIONAL – Um conjunto de atitudes e habilidades que todos, não só cientistas da computação, ficaram ansiosos para aprender e usar.**

## RESUMO

Apresenta-se aqui a tradução do trabalho intitulado "Computational Thinking", da americana Jeannette Wing, professora de Ciência da Computação e chefe do Departamento de Ciência da Computação na Universidade de Carnegie Mellon, Pittsburgh, PA, OT

## Computational Thinking

## 計算論的思考



Jeannette M. Wing (Microsoft Research and Carnegie Mellon University)

翻訳：中島秀之 (公立ほこだて未来大学)

[原文] Jeannette M. Wing : Computational Thinking, *Communications of the ACM*, Vol.49, No.3, pp.33-35 (Mar. 2006) より許可を得て翻訳。

これはWingの2006年のエッセイである。これが出た当時、我々日本の研究者仲間も似たような感覚を持っていたので、このエッセイを歓迎した。すぐに誰かが翻訳するものだと思っていたら、2014年の現在に至るまでその気配はない。書いてあることが我々研究者には当たり前だった(のでわざわざ翻訳しようと思わなかった)し、

# Spread the Word

- Help make computational thinking commonplace!

To fellow faculty, students, researchers, administrators,  
teachers, parents, principals, guidance counselors, school  
boards, teachers' unions,  
congressmen, policy makers, ...

Thank you!

# References (Representative Only)

- Computational Thinking
  - University of Edinburgh, <http://www.inf.ed.ac.uk/research/programmes/comp-think/>
  - [Wing06] J.M. Wing, “Computational Thinking,” *CACM Viewpoint*, March 2006, pp. 33-35, <http://www.cs.cmu.edu/~wing/>
- Model Checking, Temporal Logic, Binary Decisions Diagrams
  - [Br86] Randal Bryant, “Graph-Based Algorithms for Boolean Function Manipulation,” *IEEE Trans. Computers*, 35(8): 677-691 (1986).
  - [CE81] E. M. Clarke and E. A. Emerson, “The Design and Synthesis of Synchronization Skeletons Using Temporal Logic,” *Proceedings of the Workshop on Logics of Programs*, IBM Watson Research Center, Yorktown Heights, New York, Springer-Verlag Lecture Notes in Computer Science, #131, pp. 52–71, May 1981.
  - [CES86] E. M. Clarke, E. A. Emerson, and A. P. Sistla, “Automatic Verification of Finite State Concurrent Systems Using Temporal Logic Specifications,” *ACM Trans. Prog. Lang. and Sys.*, (8)2, pp. 244-263, 1986.
  - [CGP99] Edmund M. Clarke, Jr., Orna Grumberg and Doron A. Peled, *Model Checking*, [MIT Press](#), 1999, [ISBN 0-262-03270-8](#).
  - [Ku94] Robert P. Kurshan, *Computer Aided Verification of Coordinating Processes: An Automata-theoretic Approach*, Princeton Univ. Press, 1994.
  - [Pn77] Amir Pnueli, “The Temporal Logic of Programs,” *Foundations of Computer Science*, FOCS, pp. 46-57, 1977.
  - [QS82] Jean-Pierre Queille, Joseph Sifakis, “Specification and verification of concurrent systems in CESAR,” *Symposium on Programming*, Springer LNCS #137 1982: 337-351.
  - [VW86] Moshe Y. Vardi and Pierre Wolper, “An Automata-Theoretic Approach to Automatic Program Verification (Preliminary Report),” *Logic in Computer Science*, LICS 1986: 332-344.
- Computational Thinking and Biology
  - [Model Checking of a Diabetes-Cancer Model](#). H. Gong, P. Zuliani, E. M. Clarke. In CMLS 2011: 3rd International Symposium on Computational Models for Life Sciences, AIP Conf. Proc. 1371, pages 234-243, 2011.
  - [Symbolic Model Checking of Signaling Pathways in Pancreatic Cancer](#). H. Gong, Q. Wang, P. Zuliani, J. R. Faeder, M. T. Lotze, E. M. Clarke. In BiCoB 2011: 3rd International Conference on Bioinformatics and Computational Biology, March 23-25, 2011, New Orleans, LA.
  - [From Cardiac Cells to Genetic Regulatory Networks](#). R. Grosu, G. Batt, F. H. Fenton, J. Glimm, C. Le Guernic, S. A. Smolka, E. Bartocci. In CAV 2011: Proceedings of the 23rd International Conference on Computer-Aided Verification, LNCS 6806, pp. 396-411, 2011.
  - E. Bartocci, F. Corradini, M.R. Di Berardini et al. (2009) [Modeling and simulation of cardiac tissue using hybrid I/O automata](#)☆, 3149-3165. In *Theoretical Computer Science* 410 (33-34). <http://dblp.uni-trier.de/db/journals/...>
  - Radu Grosu, Scott A. Smolka, Flavio Corradini et al. (2009) [Learning and detecting emergent behavior in networks of cardiac myocytes](#), 97. In *Communications of the ACM* 52 (3). <http://dblp.uni-trier.de/db/journals/...>
  - Allesina and Pascual, “Googling Food Webs: Can an Eigenvector Measure Species' Importance for Coextinctions?”, *PLoS Computational Biology*, 5(9), September 4, 2009. <http://www.ploscompbiol.org/article/info:doi%2F10.1371%2Fjournal.pcbi.1000494>
  - Executable Cell Biology, Jasmin Fisher and Thomas A Henzinger, *Nature Biotechnology*, Vol. 25, No. 11, November 2007. (See paper for many other excellent references.)
  - [LJ07] Predicting Protein Folding Kinetics via Temporal Logic Model Checking, Christopher Langmead and Sumit Jha, WABI, 2007.
  - Systems Biology Group, Ziv Bar-Joseph, Carnegie Mellon University, <http://www.sb.cs.cmu.edu/pages/publications.html>

# References (Representative Only)

- Machine Learning and Applications
  - Christopher Bishop, *Pattern Recognition and Machine Learning*, Springer, 2006.
  - [FS99] Yoav Freund and Robert E. Schapire, “A short introduction to boosting.” *Journal of Japanese Society for Artificial Intelligence*, 14(5):771-780, September, 1999.
  - Tom Mitchell, *Machine Learning*, McGraw Hill, 1997
  - Symbolic Aggregate Approximation, Eamonn Keogh, UC Riverside, <http://www.cs.ucr.edu/~eamonn/SAX.htm> (applications in Medical, Meteorological and many other domains)
  - The Auton Lab, Artur Dubrawski, Jeff Schneider, Andrew Moore, Carnegie Mellon, <http://www.autonlab.org/autonweb/2.html> (applications in Astronomy, Finance, Forensics, Medical and many other domains)
- Computational Thinking and Astronomy
  - J. Gray, A.S. Szalay, A. Thakar, P. Kunszt, C. Stoughton, D. Slutz, J. vandenBerg, “Data Mining the SDSS SkyServer Database,” in *Distributed Data & Structures 4: Records of the 4th International Meeting*, W. Litwin, G. Levy (eds), Paris France March 2002, Carleton Scientific 2003, ISBN 1-894145-13-5, pp 189-210.
  - Sloan Digital Sky Survey @Johns Hopkins University, <http://www.sdss.jhu.edu/>
- Computational Thinking and Archaeology
  - Columbia University: <http://www.cs.columbia.edu/~atroccol/>
  - Digital Forma Urbis Romae Project: <http://www.graphics.stanford.edu/projects/forma-urbis/>
  - eHeritage Project, MSRA: <http://research.microsoft.com/en-us/collaboration/global/asia-pacific/programs/eheritage.aspx>
  - See also Marc Levoy’s digital archaeology projects: <http://www-graphics.stanford.edu/~levoy/>
  - See also UK universities: [http://en.wikipedia.org/wiki/Computational\\_archaeology#Research\\_groups\\_and\\_institutions](http://en.wikipedia.org/wiki/Computational_archaeology#Research_groups_and_institutions)
- Computational Thinking and Chemistry
  - [Ma07] Paul Madden, Computation and Computational Thinking in Chemistry, February 28, 2007 talk off <http://www.inf.ed.ac.uk/research/programmes/comp-think/previous.html>
- Computational Thinking and Economics
  - Abraham, D., Blum, A. and Sandholm, T., “Clearing algorithms for barter exchange markets: enabling nationwide kidney exchanges,” *Proc. 8th ACM Conf. on Electronic Commerce*, pp. 295–304. New York, NY: Association for Computing Machinery, 2007.
  - Conitzer, V., Sandholm, T., and Lang, J., [When Are Elections with Few Candidates Hard to Manipulate?](#) *Journal of the ACM*, 54(3), June 2007.

# References (Representative Only)

- Conitzer, V. and Sandholm, T., [Universal Voting Protocol Tweaks to Make Manipulation Hard](#). In Proceedings of the *International Joint Conference on Artificial Intelligence (IJCAI)*, 2003.
- Michael Kearns, Computational Game Theory, Economics, and Multi-Agent Systems, University of Pennsylvania, <http://www.cis.upenn.edu/~mkearns/#gamepapers>
- Algorithmic Game Theory, edited by Noam Nisan, Tim Roughgarden, Eva Tardos, and Vijay V. Vazirani, September 2007, <http://www.cambridge.org/us/catalogue/catalogue.asp?isbn=9780521872829>
- David Pennock, Yahoo! Research, Algorithmic Economics, [http://research.yahoo.com/ksc/Algorithmic\\_Economics](http://research.yahoo.com/ksc/Algorithmic_Economics)
- Computational Thinking and Journalism
  - MacArthur Foundation Digital Media and Learning Initiative: [http://www.macfound.org/site/c.1kLXJ8MQKrH/b.946881/k.B85/Domestic\\_Grantmaking\\_Digital\\_Media\\_Learning.htm](http://www.macfound.org/site/c.1kLXJ8MQKrH/b.946881/k.B85/Domestic_Grantmaking_Digital_Media_Learning.htm)
  - Kim Pearson, Poynter Online, eMedia Tidbits, May 2009: <http://www.poynter.org/column.asp?id=31&aid=164084>
  - Georgia Tech: <http://www.computation-and-journalism.com/main/>
- Computational Thinking and Law
  - The Poirot Project, <http://www.ffpoirot.org/>
  - Robert Plotkin, Esq., *The Genie in the Machine: How Computer-Automated Inventing is Revolutionizing Law and Business*, forthcoming from Stanford University Press, April 2009, Available from [www.geniemachine.com](http://www.geniemachine.com)
  - Burkhard Schafer, Computational Legal Theory, [http://www.law.ed.ac.uk/staff/burkhardschafer\\_69.aspx](http://www.law.ed.ac.uk/staff/burkhardschafer_69.aspx)
  - Stanford Computational Law, <http://complaw.stanford.edu/>
- Computational Thinking and Medicine and Healthcare
  - The Diamond Project, Intel Research Pittsburgh, <http://techresearch.intel.com/articles/Tera-Scale/1496.htm>
  - Institute for Computational Medicine, Johns Hopkins University, <http://www.icm.jhu.edu/>
  - See also Symbolic Aggregate Approximation, Eamonn Keogh, UC Riverside, <http://www.cs.ucr.edu/~eamonn/SAX.htm>
  - SM Belknap, H Moore, SA Lanzotti, PR Yarnold, M Getz, DL Deitrick, A Peterson, J Akesson, T Maurer, RC Soltysik, GA Storm, and I Brooks, Application of Software Design Principles and Debugging Methods to an Analgesia Prescription Reduces Risk of Severe Injury From Medical Use of Opioids, *Clinical pharmacology & Therapeutics*, Vol 84 No. 3, September 2008, pp. 385-392.
- Computational Thinking and Meteorology
  - Yubin Yang, Hui Lin, Zhongyang Guo, Jixi Jiang, "A data mining approach for heavy rainfall forecasting based on satellite image sequence analysisSource," *Computers and Geosciences*, Volume 33, Issue 1, January 2007, pp. 20-30, ISSN:0098-3004.
  - See also Symbolic Aggregate Approximation, Eamonn Keogh, UC Riverside, <http://www.cs.ucr.edu/~eamonn/SAX.htm>



# References (Representative Only)

- Computational Thinking (especially Machine Learning) and Neuroscience
  - Yong Fan, Dinggang Shen, Davatzikos, C., “**Detecting Cognitive States from fMRI Images by Machine Learning and Multivariate Classification,**” Computer Vision and Pattern Recognition Workshop, 2006. CVPRW '06, June 2006, p. 89.
  - T.M. Mitchell, R. Hutchinson, R.S. Niculescu, F.Pereira, X. Wang, M. Just, and S. Newman, "[Learning to Decode Cognitive States from Brain Images](#),"*Machine Learning*, Vol. 57, Issue 1-2, pp. 145-175. October 2004.
  - X. Wang, R. Hutchinson, and T. M. Mitchell, "[Training fMRI Classifiers to Detect Cognitive States across Multiple Human Subjects](#)," *Neural Information Processing Systems 2003*. December 2003.
  - T. Mitchell, R. Hutchinson, M. Just, R.S. Niculescu, F. Pereira, X. Wang, "[Classifying Instantaneous Cognitive States from fMRI Data](#)," *American Medical Informatics Association Symposium*, October 2003.
  - Dmitri Samaras, Image Analysis Lab, <http://www.cs.sunysb.edu/~ial/brain.html>
  - Singh, Vishwajeet and Miyapuram, K. P. and Bapi, Raju S., “*Detection of Cognitive States from fMRI data using Machine Learning Techniques,*” *IJCAI, 2007*.
- Computational Thinking and Sports
  - Synergy Sports analyzes NBA videos, <http://broadcastengineering.com/news/video-data-dissect-basketball-0608/>
  - Lance Armstrong’s cycling computer tracks man and machine statistics, website

# Credits

- Copyrighted material used under Fair Use. If you are the copyright holder and believe your material has been used unfairly, or if you have any suggestions, feedback, or support, please contact: [jsoleil@nsf.gov](mailto:jsoleil@nsf.gov)
- Except where otherwise indicated, permission is granted to copy, distribute, and/or modify all images in this document under the terms of the GNU Free Documentation license, Version 1.2 or any later version published by the Free Software Foundation; with no Invariant Sections, no Front-Cover Texts, and no Back-Cover Texts. A copy of the license is included in the section entitled “GNU Free Documentation license”  
([http://commons.wikimedia.org/wiki/Commons:GNU\\_Free\\_Documentation\\_License](http://commons.wikimedia.org/wiki/Commons:GNU_Free_Documentation_License))